

# 10.1

## Graphing Square Root Functions

For use with Exploration 10.1

**Essential Question** What are some of the characteristics of the graph of a square root function?

**1 EXPLORATION:** Graphing Square Root Functions

**Work with a partner.**

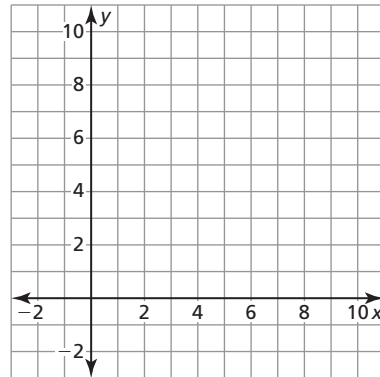
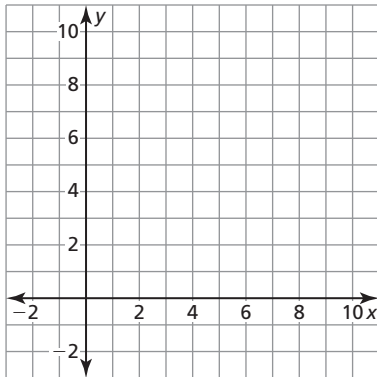
- Make a table of values for each function.
- Use the table to sketch the graph of each function.
- Describe the domain of each function.
- Describe the range of each function.

a.  $y = \sqrt{x}$

b.  $y = \sqrt{x + 2}$

<b>x</b>						
<b>y</b>						

<b>x</b>						
<b>y</b>						



**10.1** Graphing Square Root Functions (continued)

**2** **EXPLORATION:** Writing Square Root Functions

**Work with a partner.** Write a square root function,  $y = f(x)$ , that has the given values. Then use the function to complete the table.

a.

$x$	$f(x)$
-4	0
-3	
-2	
-1	$\sqrt{3}$
0	2
1	

b.

$x$	$f(x)$
-4	0
-3	
-2	
-1	$1 + \sqrt{3}$
0	3
1	

**Communicate Your Answer**

3. What are some of the characteristics of the graph of a square root function?

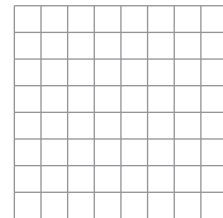
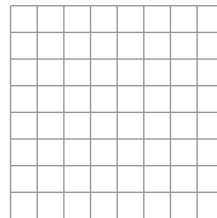
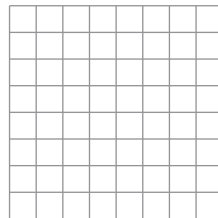
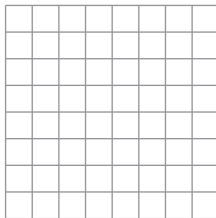
4. Graph each function. Then compare the graph to the graph of  $f(x) = \sqrt{x}$ .

a.  $g(x) = \sqrt{x - 1}$

b.  $g(x) = \sqrt{x} - 1$

c.  $g(x) = 2\sqrt{x}$

d.  $g(x) = -2\sqrt{x}$



# 10.1

## Notetaking with Vocabulary

For use after Lesson 10.1

In your own words, write the meaning of each vocabulary term.

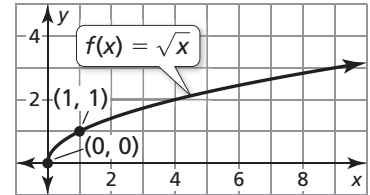
square root function

radical function

### Core Concepts

#### Square Root Functions

A **square root function** is a function that contains a square root with the independent variable in the radicand. The parent function for the family of square root functions is  $f(x) = \sqrt{x}$ . The domain of  $f$  is  $x \geq 0$ , and the range of  $f$  is  $y \geq 0$ .



**Notes:**

Transformation	$f(x)$ Notation	Examples
<b>Horizontal Translation</b> Graph shifts left or right.	$f(x - h)$	$g(x) = \sqrt{x - 2}$ <b>2 units right</b> $g(x) = \sqrt{x + 3}$ <b>3 units left</b>
<b>Vertical Translation</b> Graph shifts up or down.	$f(x) + k$	$g(x) = \sqrt{x} + 7$ <b>7 units up</b> $g(x) = \sqrt{x} - 1$ <b>1 unit down</b>
<b>Reflection</b> Graph flips over $x$ - or $y$ -axis.	$f(-x)$ $-f(x)$	$g(x) = \sqrt{-x}$ <b>in the <math>y</math>-axis</b> $g(x) = -\sqrt{x}$ <b>in the <math>x</math>-axis</b>
<b>Horizontal Stretch or Shrink</b> Graph stretches away from or shrinks toward $y$ -axis.	$f(ax)$	$g(x) = \sqrt{3x}$ <b>shrink by a factor of <math>\frac{1}{3}</math></b> $g(x) = \sqrt{\frac{1}{2}x}$ <b>stretch by a factor of 2</b>
<b>Vertical Stretch or Shrink</b> Graph stretches away from or shrinks toward $x$ -axis.	$a \cdot f(x)$	$g(x) = 4\sqrt{x}$ <b>stretch by a factor of 4</b> $g(x) = \frac{1}{5}\sqrt{x}$ <b>shrink by a factor of <math>\frac{1}{5}</math></b>

**Notes:**

**10.1** Notetaking with Vocabulary (continued)**Extra Practice**

In Exercises 1–3, describe the domain of the function.

1.  $y = 4\sqrt{-x}$

2.  $y = \sqrt{x-3}$

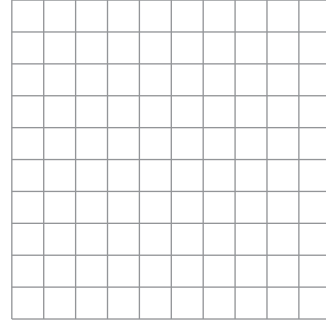
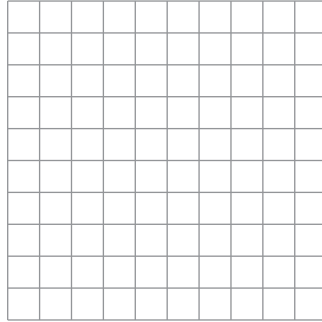
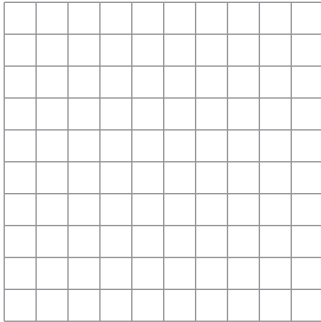
3.  $f(x) = \sqrt{\frac{1}{3}x} + 4$

In Exercises 4–6, graph the function. Describe the range.

4.  $y = \sqrt{3x}$

5.  $y = 2\sqrt{-x}$

6.  $g(x) = \sqrt{x+3} - 1$



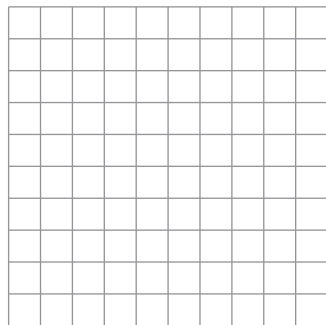
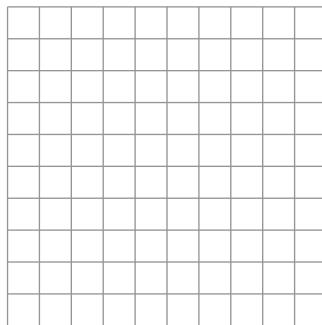
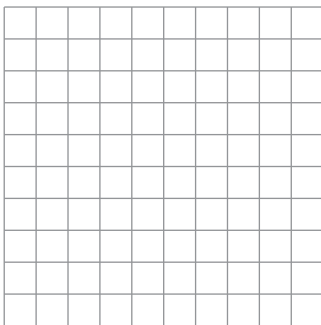
In Exercises 7–9, graph the function. Compare the graph to the graph of

$f(x) = \sqrt{x}$ .

7.  $r(x) = \sqrt{-\frac{1}{2}x}$

8.  $s(x) = -\sqrt{x} - 2$

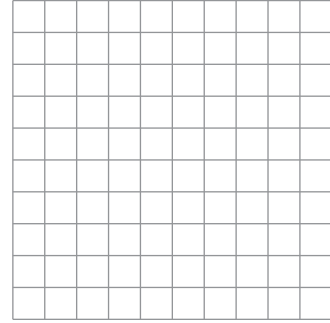
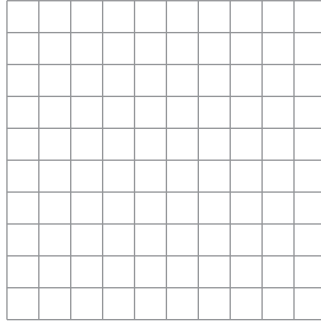
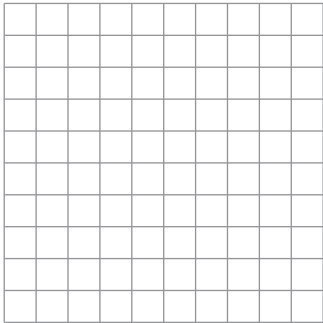
9.  $t(x) = \sqrt{x+4}$



**10.1** Notetaking with Vocabulary (continued)

In Exercises 10–12, describe the transformations from the graph of  $f(x) = \sqrt{x}$  to the graph the of  $h$ . Then graph  $h$ .

10.  $h(x) = \frac{1}{2}\sqrt{x+2} - 2$     11.  $h(x) = 2\sqrt{x-3} + 1$     12.  $h(x) = -\sqrt{x+4} - 4$



13. The model  $S(d) = \sqrt{30df}$  represents the speed  $S$  (in miles per hour) of a car before it skids to a stop, where  $f$  is the drag factor of the road surface and  $d$  is the length (in feet) of the skid marks. The drag factor of Road Surface C is 0.8. The graph shows the speed of the car on Road Surface D. Compare the speeds by finding and interpreting their average rates of change over the interval  $d = 0$  to  $d = 20$ .

