

Name: \_\_\_\_\_

Date: \_\_\_\_\_

# 1A Exercises

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## Finding Limits Graphically & Numerically

Complete the table and use the result to estimate the limit. Use a graphing utility to graph the function to confirm your result. Sketch the graph in the neighborhood of the limit point.

1.  $\lim_{x \rightarrow 4} \frac{x - 4}{x^2 - 3x - 4}$

$x$	3.9	3.99	3.999	4.001	4.01	4.1
$f(x)$						

5.  $\lim_{x \rightarrow 3} \frac{[1/(x + 1)] - (1/4)}{x - 3}$

$x$	2.9	2.99	2.999	3.001	3.01	3.1
$f(x)$						

7.  $\lim_{x \rightarrow 0} \frac{\sin x}{x}$

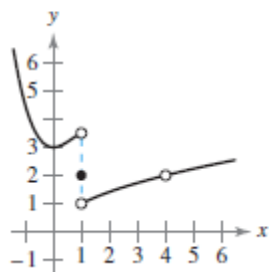
$x$	-0.1	-0.01	-0.001	0.001	0.01	0.1
$f(x)$						

8.  $\lim_{x \rightarrow 0} \frac{\cos x - 1}{x}$

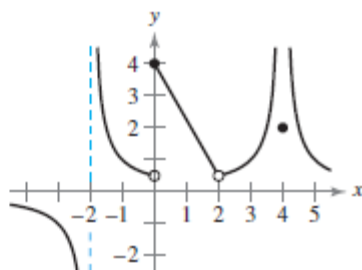
$x$	-0.1	-0.01	-0.001	0.001	0.01	0.1
$f(x)$						

In Exercises 25 and 26, use the graph of the function  $f$  to decide whether the value of the given quantity exists. If it does, find it. If not, explain why.

25. (a)  $f(1)$   
 (b)  $\lim_{x \rightarrow 1} f(x)$   
 (c)  $f(4)$   
 (d)  $\lim_{x \rightarrow 4} f(x)$



26. (a)  $f(-2)$   
 (b)  $\lim_{x \rightarrow -2} f(x)$   
 (c)  $f(0)$   
 (d)  $\lim_{x \rightarrow 0} f(x)$   
 (e)  $f(2)$   
 (f)  $\lim_{x \rightarrow 2} f(x)$   
 (g)  $f(4)$   
 (h)  $\lim_{x \rightarrow 4} f(x)$



In Exercises 31 and 32, sketch a graph of a function  $f$  that satisfies the given values. (There are many correct answers)

31.  $f(0)$  is undefined.

$$\lim_{x \rightarrow 0} f(x) = 4$$

$$f(2) = 6$$

$$\lim_{x \rightarrow 2} f(x) = 3$$

32.  $f(-2) = 0$

$$f(2) = 0$$

$$\lim_{x \rightarrow -2} f(x) = 0$$

$$\lim_{x \rightarrow 2} f(x) \text{ does not exist.}$$