

7a.1-SSA... The Ambiguous Case

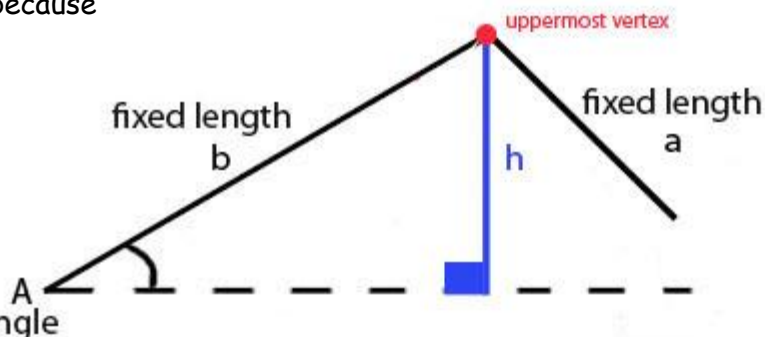
When we have a Side-Side-Angle situation, the law of Sines is not guaranteed to give us the *only* solution because when we take the inverse sine, there are more than one possible angle.

For an acute angle A

Suppose we are given angle A , side b , and side a like in the drawing to the right.

This will only make a triangle if the side a is longer than the height h .

As we have seen before, the height can be found using $h = b \sin A$. So, we get three cases:



| Relationship of a and $h = b \sin A$ | Number of Triangles |
|--|---|
| $b \sin A > a$ | 0 possible triangles |
| $b \sin A < a$ and $b < a$ | 1 possible triangle |
| $b \sin A < a$ and $b > a$ | 2 possible triangles |
| $b \sin A = a$ | 1 possible triangle... it's a right triangle! |

For an obtuse angle A

When we have an obtuse angle A , we simply need the opposite side a to be greater than b .

| | |
|---------|----------------------|
| $a < b$ | 0 possible triangles |
| $a > b$ | 1 possible triangle |

Extra Practice

- Decide if there are one, two, or no possible triangles with the given measurements. Explain and show any work.
 - $a = 9, b = 7, A = 108^\circ$
 - $a = 14, b = 15, A = 117^\circ$
 - $a = 5, b = 12, A = 27^\circ$

d. $a = 35, b = 24, A = 82^\circ$

e. $a = 19, b = 38, A = 30^\circ$

f. $a = 6, b = 6, A = 63^\circ$

g. $a = 10, b = \sqrt{200}, A = 45^\circ$

2. Find two triangles with the given angle measure and side lengths. Round side lengths to the nearest tenth and angle measures to the nearest degree.

$$A = 39^\circ, a = 12, b = 17$$