



# 3.1: Measures of Center: *One Number to Represent the Group*

## Home Values in a Subdivision

Data: \$125k, \$125k, \$132k, \$138k, \$142k, \$584k

- ⦿ So, what is the “Typical price of a home in this subdivision?”
- ⦿ Who might need an average value?
- ⦿ There is more than one way to find an average.

## Mean

- ⦿ The mean ( $\bar{x}$  – read “x-bar”) is the sum of the observations divided by the number of observations
- ⦿ It is the center of mass

**Example:** Data: 24,12, 45, 33, 56, 62,14, 28

$$\bar{x} = \frac{\sum x}{n}$$

- ⦿  $Mean(\bar{x}) = \frac{\text{sum of the } x\text{'s}}{\text{number of data points } (n)}$
- ⦿  $Mean = \frac{24+12+45+33+56+62+14+28}{8} = 34.25$

## Median

- ⦿ The median is the midpoint of the observations when they are ordered from the smallest to the largest (or from the largest to smallest)
- ⦿ Order observations
- ⦿ If the number of observations is:
  - Odd, then the median is the middle observation
  - Even, then the median is the average of the two middle observations

### Example:

Find the sample size,  $n$ ,  
and the median.

Order	Data	Order	Data
1	78	1	78
2	91	2	91
3	94	3	94
4	98	4	98
5	99	5	99
6	101	6	101
7	103	7	103
8	105	8	105
9	114	9	114
		10	121

**Try It:**

**CO<sub>2</sub> Pollution levels in 8 largest nations measured in metric tons per person:**

**2.3 1.1 19.7 9.8 1.8 1.2 0.7 0.2**

**Find the mean and Median.**

**Mean:**

**Median:**

**Mode**

- Value that occurs most often
- Highest bar in the histogram
- The mode is most often used with categorical data

**Try it :** Find the mean of these data sets

	Mean	Median	Mode
Set 1: 1, 2, 3, 4, 5			
Set 2: 1, 1, 2, 3, 102			
Set 3: 1, 1, 1, 1, 1, 2, 4, 69			

**Think about this:** Which measure of center best describes each data set?

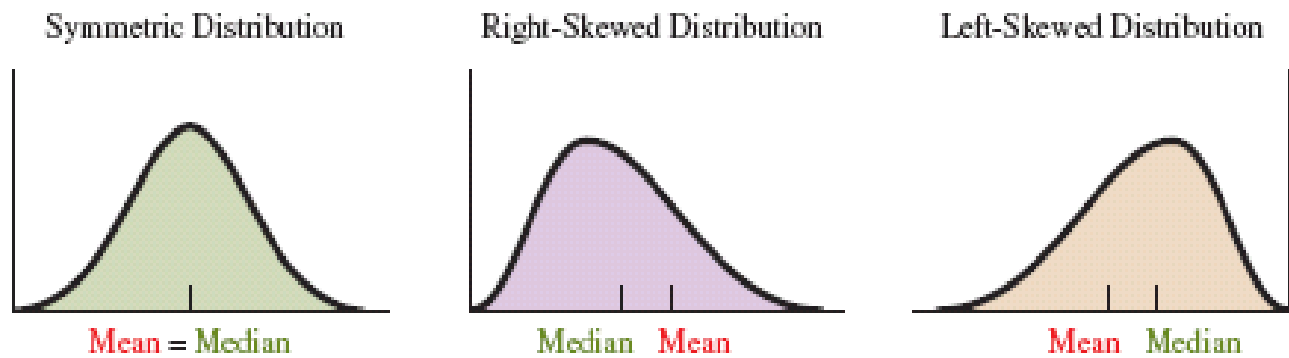
**Set 1:**

**Set 2:**

**Set 3:**

## Comparing the Mean and Median

- ⦿ The mean and median of a symmetric distribution are close together.
  - For symmetric distributions, the mean is typically preferred because it takes the values of all observations into account
- ⦿ In a skewed distribution, the mean is farther out in the long tail than the median
  - For skewed distributions the median is preferred because it is better representative of a typical observation



- ⦿ A numerical summary measure is resistant if extreme observations (outliers) have little, if any, influence on its value
  - The Median is resistant to outliers
  - The Mean is not resistant to outliers